Chapter 27

Phasing An Image Using Non-Linear Phases

The phasing algorithm presented in Chapter 26 can phase any NMR image in which the phases vary linearly in both domains. Consequently that phasing algorithm works well for spin echo and EPI images, but it does not work for gradient echos because in gradient echos the phase varies non-linearly. This effect is illustrated in Fig. 27.1 panels (A) and (B). The linear phasing algorithm has removed most of the oscillations, but has left behind a slowly varying phase that causes the signal to oscillate between the real and imaginary channels. In Panel (C) and (D) we have displayed the real and imaginary images after the nonlinear phasing routine has been run. The nonlinear phasing routine has moved all of the image from the imaginary changes into the real channel and left behind what appears to be white noise. Indeed if you compute the standard deviation of the noise from a region that contains no signal in the real and imaginary images, you will find they are nearly identical. In this chapter we describe the interface to the nonlinear phasing package, BayesPhase2, and give the calculations needed to phase a gradient echo.

27.1 The Model Equation

As in all Bayesian calculations, the calculations begin by relating the parameters of interest to the data, i.e., by stating the model. The model we are going to use is a pixel model. That is to say, we will use exactly the same model on every pixel and each pixel will be treated independently of ever other pixel. Because each pixel is being treated separately, if the image is 128 by 256 then there are a total of 32K different calculations that must be performed. However, each calculation involves only one complex data and two parameters so the calculations are very fast.

Because the discrete Fourier transform is an information preserving transformation, it does not mater if we do the calculation in the time or image domain; both calculations are equivalent. For convenience we will present this calculation in the image domain. What we wish to do is to determine how uncertain we are of both the phase and the amplitude in each pixel and then use the phase to generate a phased image. In a real sense we are not interested in either the amplitude and phase, rather we are interested in how uncertain we are of these quantities, because the resulting phased image must reflect these uncertainties.
Figure 27.1: Nonlinear Phasing Example

(A) Linear Phases, the Real image

(B) Linear Phases, the Imaginary image

(C) Non-Linear Phases, the Real image

(D) Non-Linear Phases, the Imaginary image

Figure 27.1: Panels (A) and (B) are the real and imaginary images generated from a gradient echo when the linear phasing algorithm is used. Note that the imaginary image, panel (B), still has a strong signal. This signal oscillates positive and negative in both the real and imaginary images. Panel (C) is the real image generated by the nonlinear phasing algorithm. The imaginary image (D) is essentially noise. If you compute the standard deviation of the noise from a section of the real and imaginary images you find they are essentially identical; indicating that the image is almost perfectly phased.
If \( d \) represents a complex image pixel value, then the model for any given pixel is

\[
d = A \exp \{ -i\theta \} + n \tag{27.1}
\]

where \( A \) is the amplitude of the image and \( \theta \) is the phase. The quantity \( n \) represents the noise, and in this calculation we will assume the standard deviation of the noise, \( \sigma \), is known. Separating the real and imaginary parts of this signal one has

\[
d_R = A \cos(\theta) + n_R \tag{27.2}
\]

for the real channel and

\[
d_I = -A \sin(\theta) + n_I \tag{27.3}
\]

for the imaginary channel, where \( d_R \) and \( d_R \) represent the real and imaginary pixel values and \( n_R \) and \( n_I \) represent the real and imaginary noise values. In the calculations which follow it will be assumed that the standard deviation of the noise is the same in both the real and imaginary channels and that the noise values are the same over the entire image.

### 27.2 The Bayesian Calculations

The Bayesian calculation consists of applying Bayes’ theorem

\[
P(A\theta|\sigma d_R d_I) = \frac{P(A\theta|\sigma I)P(d_R d_I|\sigma A\theta I)}{P(d_R d_I|\sigma I)} \tag{27.4}
\]

where \( P(A\theta|\sigma I) \) is the joint posterior probability for the parameters given the noise standard deviation, the data and the prior information \( I \). The joint prior probability for the parameters, \( P(A\theta|\sigma I) \), represents what was known about these parameters before the data were acquired. The direct probability for the data, \( P(d_R d_I|\sigma A\theta I) \), is essentially the likelihood function and \( P(d_R d_I|\sigma I) \) is a normalization constant. If we normalize this probability density function at the end of the calculation and factor the joint prior probability for the parameters, one obtains

\[
P(A\theta|\sigma d_I) \propto P(A|I)P(\theta|I)P(d|A\theta I) \tag{27.5}
\]

as the joint posterior probability for the parameters.

In this calculation we will assign independent prior probabilities for the amplitude and Phase. And the likelihood will be assigned using a Gaussian prior probability. By definition the amplitude should be positive, but we do not wish to insert a hard lower bound on the amplitude. The reason for this is that in this analysis we are not doing a model selection calculation; rather we are doing a parameter estimation calculation. If we were doing a model selection calculation, then we could select between Eq. (27.1) and the “no signal” model. If we had done that then a hard cutoff would have worked fine as the prior probability. In regions where there is no signal, we would just get noise, and in regions where the signal is large we would get a properly phased signal. However, if we are doing parameter estimation, then a hard lower bound will necessarily force the real image to be positive, and so put a constant offset into the image: exactly the same thing that happens when one uses and absolute image. Consequently, we will use a prior that strongly suggests the amplitude
should be positive:

\[
P(A|\sigma I) \propto \begin{cases} 
\exp \left[ -\frac{A^2}{2\sigma^2} \right] & \text{if } A < -3\sigma \\
\exp \left[ -\frac{A^2}{2\delta^2} \right] & \text{otherwise}
\end{cases}
\]  \hspace{1cm} (27.6)

where \( \delta \) is one half the maximum intensity in the image. So this prior expresses the belief that the amplitude should be small rather than large. Around zero this prior has almost no effect on negative amplitudes until the amplitude become more negative than three noise standard deviations, then suddenly this prior expresses a rather strong belief that the amplitude should be closer to zero. So small negative values are allowed, provided they are small enough not to protrude above the noise floor.

The prior probability for the phase is also assigned using a Gaussian prior probability of the form:

\[
P(\theta|I) \propto \exp \left\{ -\frac{\theta^2}{2 \times 2^2} \right\}.
\]  \hspace{1cm} (27.7)

This prior expresses a slight belief that the phase should be zero. The reason for this is simply that noise does not really have a phase, and so the phase should be zero. Any data item having even a small significant amplitude will quickly override this prior.

The likelihood, \( P(d_Rd_I|A\theta\sigma I) \) was assigned using a Gaussian given by

\[
P(d_Rd_I|A\theta\sigma I) \propto \exp \left\{ -\frac{Q^2}{2\sigma^2} \right\}
\]  \hspace{1cm} (27.8)

where

\[
Q \equiv |d_R - A\cos(\theta)|^2 + |d_I + A\sin(\theta)|^2.
\]  \hspace{1cm} (27.9)

In the program that implements the calculation, the noise standard deviation \( \sigma \) must be determined. There are many ways this might be done, but whatever is done, it must be general enough to work on any image. If you examine the output from the linear phasing routine, Fig. 27.1 panels (A) and (B), you will note that in small patches of the image, say \( 3 \times 3 \) pixels, the signal in the real and imaginary channels are roughly constant; different constants in the real and imaginary, but constant nonetheless. If you postulate a model that is a constant in this small region and then compare the constant model to the “no signal” model, one can compute the posterior probability for these two models. If there is no signal present, then that region can be used to compute the noise standard deviation. By going over the entire image using a \( 3 \times 3 \) set on pixels one can quickly get a very accurate estimate of the noise standard deviation by using only pixels for which the probability for no signal is much greater that the probability for the constant model.

The Bayesian calculations are implemented using Markov chain Monte Carlo, without simulated annealing. The Markov chain has Eq. (27.5) as its target distribution, using Eqs. (27.6,27.7) as the prior probabilities and Eq.(27.8) as the direct probability. The calculations are implemented in parallel, with parallelization occurring at the pixel level. Consequently, it 32 processors are available then 32 pixels are processed at one time. The simulations are initialized using the maximum likelihood estimated of both the amplitude and phase. Consequently, these simulations start very near the maximum of the joint posterior probability and all that is necessary is to run the simulations long enough for them to reach equilibrium.
In most Markov chain Monte Carlo simulations, it is the means and standard deviations of the parameter samples that are output. If we had used the mean phases to generate the output image, we would almost certainly get the maximum of the direct probability in regions where there is a signal, and, consequently, the output would essentially be an absolute value spectrum. However, we are not trying to estimate the amplitudes and phases, we are trying to phase an image. In the Markov chain Monte Carlo simulations each of the samples from the simulations are characteristic of the phase and amplitude supported by the data. Consequently, we randomly take one phase from one of the Markov chain Monte Carlo simulations and use that phase to produce an absorption mode pixel. This process is repeated for each pixel, giving an absorption model image. Figure 27.1 panels (C) and (D) are the real and imaginary parts of a gradient echo image that was phased using this procedure. Note that the real image (C) contains the fully phased image, plus noise; while the imaginary image (D) contains only noise. If one computes the noise standard deviation for these two images one finds essentially the same value in both real and imaginary images, and this value is the same as what is found in both panels (A) and (B), the real and imaginary parts of the linearly phased image; so this procedure has moved the positive intensity to the real channel and left the noise behind.

27.3 The Interfaces To The Nonlinear Phasing Routine

The interfaces to the Nonlinear Phasing package are shown in Fig. 27.2. To use this package you must:

- Run the linear phasing algorithm and have that package write both the imaginary and real FDF images.
- Select the type of processing:
  - **All**: all of images are to be phased separately.
  - **One**: only the currently displayed image is to be phased.
  - **Common**: the phase from the currently displayed image are to be computed, and those phases are then used on all of the images.
- Indicate if the imaginary images are to be written, the default is not to write these images.
- Indicate if the Ascii image are to be written, the default is not to write these images.

The remaining widgets on this interface are used to view the outputs and to indicate where the analysis is to be run. These widgets are pretty standard and we do not discuss them further. If you need to know more about the function of these widgets activate the help button and then activate the widget in question.
Figure 27.2: The Interface To The Nonlinear Phasing Package

To use the Bayes Phase package:

1. Load the image you wish to phase.
2. Select the processing to All or Common.
3. Set the noise standard deviation.
   a. Draw an ROI in the noise
   b. Generate the statistics for that ROI
   c. Copy the standard deviation into the "Noise SD" entry box
4. Select the server to run the analysis.
5. Run the analysis using the "Run" button.
6. Use "Get Job" to get the results from the server.

Figure 27.2: The interface to the Nonlinear phasing package is shown here. The output from this package is the phased real and imaginary parts of the input image. These images, usually just the real image, can be used in other analysis such as inversion recovery and diffusion tensor packages.
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