

Bayesian Data-Analysis Toolbox
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Appendix B

Markov chain Monte Carlo With Simulated Annealing

Most of the packages in the Bayesian Analysis software use Markov chain Monte Carlo simulations to approximate the Bayesian posterior probability. To understand how a Markov chain can be used to do this, suppose there is some quantity called M . This quantity could be a set of parameters or it could be a selection of models and the object of the Bayesian calculation is to estimate the parameters or to determine which model best characterizes the data. While these two problems sound very different, they are really one and the same problem. To see this suppose M is just the decay rate constant in a simple exponential decay, then discrete values of M , just specify a set of models $\{M_1, M_2, \dots, M_n\}$ and in parameter estimation we compute the posterior probability for each model, just as we do in model selection. So model selection and parameter estimation are fundamentally the same problem. The major difference is that in parameter estimation problems, the functional form of the models is the same, while it can be different in model selection.

The estimation problems addressed by the various packages are all structurally similar, suppose M consists of a set of parameters or model indicators, $M \in \{M_1, M_2, \dots, M_n\}$, and we wish to compute the posterior probability for an individual parameters $P(M_j|DI)$ where M_j is the hypothesis of interest, D represents all of the data and I is the prior information. Applying the rules of Bayesian probability theory, the joint posterior probability for all of the parameters is given by

$$P(M_1 \dots M_n | DI) = \frac{P(M_1 \dots M_n | I) P(D | M_1 \dots M_n I)}{P(D | I)} \quad (\text{B.1})$$

which is Bayes' theorem [1]. For those unfamiliar with the rules of Bayesian probability theory, see Chapter ?? for a tutorial on probability theory or consult [31, 3, 11, 33, 61, 32] for more detailed descriptions of probability theory when treated as extended logic.

If we normalize this posterior probability at the end of the calculation, then $P(D|I)$ can be dropped and one obtains:

$$P(M_1 \dots M_n | DI) \propto P(M_1 \dots M_n | I) P(D | M_1 \dots M_n I). \quad (\text{B.2})$$

Using logical independence and the product rule, the joint prior probability, $P(M_1 \dots M_n | DI)$, can

be factored to obtain

$$P(M_1 \dots M_n | DI) \propto P(M_1 | I) \dots P(M_n | I) P(D | M_1 \dots M_n I) \quad (\text{B.3})$$

and it is this joint posterior probability that most of the Markov chain Monte Carlo simulation approximate. To determine exactly how an individual package implements this calculation, see the Chapter describing that package.

If all a Markov chain Monte Carlo simulation did was to approximate this joint posterior probability, it would not be very useful because what is really needed in the Bayesian calculation is not $P(M_1 \dots M_n | DI)$, but $P(M_j | DI)$ where $P(M_j | DI)$ is computed using the sum rule of probability theory:

$$P(M_j | DI) = \int_{M_1} \dots \int_{M_n} P(M_1 | I) \dots P(M_n | I) P(D | M_1 \dots M_n I) dM_1 \dots dM_n \quad (\text{B.4})$$

where the integrals are over all M_i except j . In the Markov chain Monte Carlo simulation this part of the calculation is done using Monte Carlo integration which consists of sampling the joint posterior probability, the integrand, and then using the samples for each parameter as samples from the marginal posterior probability for each parameter separately.

B.1 Metropolis-Hastings Algorithm

All of the packages that implement their calculations using Markov chain Monte Carlo use the **Metropolis-Hastings** algorithm and you can read more about the Metropolis-Hastings algorithm at the previous Wikipedia link. You can consult the original 1953 paper [45] paper, Gilks et al. have written extensively on Markov chain Monte Carlo as used in Bayesian probability theory [24] and Radford Neal did his dissertation on that subject [46]. Here we will briefly summarize how the Metropolis-Hastings algorithm is used to approximate the Bayesian posterior probabilities.

At their heart all Markov chain simulations are random number generators in which you, the author, can choose the distribution of the random numbers. In the Bayesian calculations done in this software the chosen distribution is the joint posterior probability for all of the parameters and model indicators given the data and the prior information. By running the chain one can sample the joint posterior probability built into the Markov chain simulation. To run a Markov chain Monte Carlo simulation, one must be able to compute Eq. (B.3) for a given set of parameters and model indicators. Here is a very toy version of how one runs a Markov chain Monte Carlo simulation to sample the joint posterior probability:

1. One begins the process of generating a Markov chain by simply sampling the parameter from their valid range. We are going to call these parameters M_0 and the joint posterior probability computed using M_0 will be designated as P_0 .
2. Next propose a new value for one or more of the parameter. Call this new proposed set of parameters M_1 , and compute the joint posterior probability, P_1 using the proposed values.
3. Accept the proposal if P_1 is greater than P_0 . Here accepting the proposal means that you replace M_0 and P_0 by M_1 and P_1 respectively and go back to Step 2.

4. If P_1 is less than or equal to P_0 , then draw a random number, r , from a uniform $(0-1)$ random number generator, and if the ratio P_1/P_0 is greater than r , accept the proposed value of P_1 and M_1 , i.e., replace M_0 and P_0 with M_1 and P_1 and go to Step 2.
5. Otherwise, reject the proposed values. Here rejecting the proposed values simply means going back to Step 2 without replacing M_0 or P_0 .

This simple 5 step procedure is all it takes to generate a Markov chain Monte Carlo simulation. Unfortunately, implementing the calculation in practice, is more of an art than a science and, shortly, we will describe a few of the tricks used in ensuring the calculations work correctly.

There are several major problems with the Markov chain Monte Carlo simulation as described so far: First, it is possible for the simulation to become stuck in local maxima and one would never know it. So one needs a mechanism for detecting simulations that are trapped in local maxima. Second, even if the chain converges correctly its very difficult to tell if the Markov chain has reached a stationary point. One can run a single chain over multiple steps and then look at the path of the simulation, but this is a very unreliable method of testing whether or not a simulation has converged because simulations often deviate from the maximum. And third, with a single chain it is very difficult to adjust the acceptance rate, the number of times a change to a simulation is accepted divided by the total number of times one changed the simulation.

In the following sections we are going to describe how multiple simulations, simulated annealing, killing simulations and adjusting the rate of acceptance in the simulation can be used to generate Markov chains that are highly robust, and almost impossible to get stuck in a local maxima.

B.2 Multiple Simulations

We do not run a single Markov chain Monte Carlo simulation; rather we run an ensemble of simulations in parallel. Typically, the ensemble is on the order of a few 10's, for example the defaults number of simulations used in the interface is 50, 50 because experience with running multiple simulations indicates that most of the time 50 simulations is enough to explore most parameter spaces; while running fewer increases the risk of nonconvergence and running more usually make things run longer without improving convergence.

For reasons that will become apparent shortly, we initialize the simulations from the prior probability for the parameters. We then run the simulations through a fixed number of steps. Here running a simulation means that we vary the parameters in one simulation, and then either accept or reject the modified simulation based on the prescription given above, Section B.1. This procedure is repeated for each parameter in each simulation and we repeat this procedure at least 25 times for each parameter. So for example if there are 50 simulations, 20 parameters, and each parameter is varied 25 times, the operations count is about $50 \times 20 \times 25 = 25,000$ operations to bring the ensemble of simulations to equilibrium.

Between annealing steps various statistics are computed from the multiple simulations and these statistics are used to aid in judging convergence. Additionally, the expected value of the logarithm of the likelihood is used in thermodynamic integration, Section C, and the trajectories of each simulation are good visual aids in determining convergence.

B.3 Simulated Annealing

These simulations are run using simulated annealing. In simulated annealing one introduces an annealing parameter, which we call β , into the calculation of the joint posterior probability, Eq. (B.3). This annealing parameter is introduced by raising the direct probability for the data to the β power:

$$P(M_1 \dots M_n | \beta D I) = P(M_1 | I) \dots P(M_n | I) P(D | M_1 \dots M_n I)^\beta \quad (\text{B.5})$$

where we have modified the notation to indicate that the joint posterior probability is a function of β . It is this modified joint probability density function that is used in the Markov chain Monte Carlo simulation. When $\beta = 0$, the likelihood is raised to the power of zero and the data completely disappears from the problem, one is sampling the prior. Consequently, when the Markov chain Monte Carlo simulations are initialized they are initialized from the prior probability for the parameters. Also note, that when $\beta = 1$ we are sampling the full joint posterior probability for the parameters and model indicators. The annealing parameter, β , is varied from zero to one according to some annealing schedule, discussed shortly.

Typically one starts the simulations with $\beta = 0$ and runs the simulations until they reach equilibrium. Running the simulations means changing the parameters in a simulation and then accepting or rejecting the change according to the simple perception given earlier, Chapter B.1. For a given value of β , when running the simulations, the posterior probability will increase to an equilibrium point. That is to say, the posterior probability will quit increasing and simply fluctuate about the peak in the posterior probability.

Once the simulations are in equilibrium, we increase the annealing parameter by small amount. This has the effect of knocking the ensemble of simulations out of equilibrium, so we again run the simulations until they reach equilibrium at this new value of β . When the annealing parameter is increased, the likelihood becomes more important and the simulations will begin to cluster around the high likelihood regions. However, because the annealing parameter is still small, the simulations will explore a much larger part of parameter space simply because the likelihood is not let strongly constraining them. As the annealing parameter is increased the likelihood becomes increasingly important and the simulations begin to cluster about increasingly high and higher likelihood regions.

B.4 The Annealing Schedule

The annealing schedule, the way the annealing parameter β is varied from zero to one, can be something as simple as varying the annealing parameter linearly to something much more elaborate. In earlier versions of the software, a linear annealing schedule was used. In a linear annealing schedule the annealing parameter was given by:

$$\beta = \frac{j}{n} \quad (0 \leq j \leq n) \quad (\text{B.6})$$

where n is the number of nonzero steps taken in the annealing. This worked well for many problems, but sometimes ran into difficulty when the logarithm of the likelihood is very rapidly changing, because the first tentative steps in simulated annealing can raise the likelihood many hundreds of orders of magnitude and consequently the simulations can fail to local the global maximum of the posterior probability.

In the current version of the software the annealing parameter is adjusted dynamically as follows. The annealing parameter starts at zero, and the simulations are run until they reaches equilibrium. Call this step n . For the next step, the $n + 1$ step, the annealing parameter is given by

$$\beta_{n+1} = \text{Min}(1, \beta_n + d\beta_n) \quad (\text{B.7})$$

where β_{n+1} is the value of β to be used in the next annealing step. If the minimum number of annealing steps is N , then $d\beta$ is given by:

$$d\beta = \text{Min} \left(\frac{1}{\sigma + N}, 1 - \beta \right) \quad (\text{B.8})$$

where σ is the standard deviation of the logarithm of the likelihood computed from the ensemble of simulations. Note that if the standard deviation of the logarithm likelihood is small, then this method of computing β just reduces to Eq. (B.6), i.e., a linear annealing schedule. However, when the simulations are first initialized by sampling the prior probability for the parameters, the standard deviation of the logarithm of the likelihood is usually large, and consequently, the simulations initially move slowly, gaining speed as the simulations converge on the global maxima.

It is this initial slow annealing that allows the multiple Markov chain simulations to explore the parameter space and locate the global maximum of the posterior probability. However, slowing the annealing down at small values of β is not enough to ensure that the simulations reach the global maximum; it is still possible for simulations to become stuck in local maxima.

B.5 Killing Simulations

As noted, slowing down the annealing for small values of β works very well for giving the simulations time to find the global maxima. However, it is not enough, it is still possible for simulations to become stuck in a local maxima. These trapped simulations must be found and fixed as quickly as possible if the simulations are to reach a stationary point.

Up to now the Markov chain simulations have been described as having multiple chains running in parallel using simulated annealing with an annealing parameter set dynamically based on the standard deviation of the logarithm of the likelihood. Each step in the Markov chain proceeds roughly as follows, the value of the annealing parameter is computed and set for this step in the simulated annealing cycle. Prior to setting to the annealing parameter, simulations should be in a equilibrium. However, incrementing the annealing parameter throws the simulations out of equilibrium and because the simulations are out of equilibrium, we make a number of other modifications to the simulations, we adjust the rate of acceptance, and we kill off a number of simulations.

Between annealing steps, the algorithm doing the Markov chain simulation kills off low probability simulations. To do this the algorithm computes the logarithm of the posterior probability for each simulation. This table of logarithms is then indexed, sorted, and used to replace low probability simulations. In this step typically 10% of the simulations are replaced by higher probability simulations. The program simply takes the lowest probability simulation and then replaces the simulation by one of the simulations having higher probability. The higher probability replacement is chosen by drawing a random number from a Gaussian having a standard deviation that is roughly one third of the total simulations. So when a simulation is replaced, it is replaced by a higher probability simulation, but not necessarily the highest probability simulation.

B.6 the Proposal

When doing a Metropolis-Hastings Markov chain Monte Carlo simulation one must be careful in proposing new values of a parameter. If the current value of a parameter is M_0 , one proposes a new parameter value M_1 as follows:

$$M_1 = M_0 + \delta M \quad (\text{B.9})$$

where δM is the change that is being made to the parameter. The exact method one obtains this δM doesn't matter except for one propriety that must be enforced. If the probability of moving from M_0 to M_1 is given by $P(M_1|M_0I)$ then the probability of moving from M_1 to M_0 must be the same:

$$P(M_0|M_1I) = P(M_1|M_0I) \quad (\text{B.10})$$

That is to say jumps in the proposal probability must be symmetric. There are countless modifications and addendum to this rule and you can look at the various references on Markov chain simulations on what these modifications are, but in the calculations implemented in this software package, Eq. (B.10) is the rule implemented using a simple Gaussian proposal. A Gaussian proposal has a number of advantages, for example it is symmetric in its argument and thus automatically satisfies Eq. (B.10). Additionally, a Gaussian has one additional parameter that is important, its standard deviation. By adjusting the size of the standard deviation of the proposal one can control how often the Markov chain transitions from one proposed value to another.

Now one might ask why this is important and the answer is simple, if the proposal is too small the simulation will not explore the parameter space and if the proposal is too large, the change in the posterior probability will be so great that the probability of accepting the change is zero and again the simulations do not explore the parameter space. Consequently, it is important to monitor the size of the proposal and to adjust it between annealing steps to ensure it is neither too small or too large.

The way the programs that implement the Markov chain simulations control the proposal is by keeping track of the acceptance rate for a given parameter. The acceptance rate is simply the ratio of the number of times a proposed parameter was accepted divided by the total number of times one proposed a new parameter value. There is not hard and fast rule on how often one should accept a parameter, but too often or too little are both bad. Additionally, if one is to error, then err on the side of more exploration of the parameter space is probably a good thing. Consequently, the programs that implement these calculations try and keep the acceptance rate between 20 and 30%. If the acceptance rate falls below 20% the proposal is decreased and if the acceptance rate is above 30% the proposal is increased. If it is between 20 and 30% no change is made. There are many addendum that could be added to this description, but it captures what the program actually does. Indeed, there is an output report generated by most of the packages in the Bayesian Analysis Software called an accepted report and that report is available while a package is running and needless to say, its primary output is the current acceptance rate for the various parameters.

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